POWER SYSTEM DYNAMIC STABILITY ASSESSMENT USING FUZZY ARTMAP NEURAL NETWORK

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Abstract: This paper presents the application of Fuzzy ARTMAP neural network for evaluating on-line power system dynamic stability.

Using the matrix transformation of the S-matrix method, the absolute value of the most critical eigenvalue in Z-plane has been regarded as dynamic stability index of power system.

For evaluation of dynamic stability indices, a typical power system is tested and the results are compared with those obtained from classical multi-layer Perceptron. For on-line training, the Fuzzy ARTMAP network is found to be a better choice than the other neural networks. Also it is shown that the Fuzzy ARTMAP network has low sensitivity to the number of data set selection, which is used for training, and to the number of input bits.

Keywords: Power Systems, Dynamic Stability, Fuzzy ARTMAP Neural Network

1. Introduction

An important task in power system operation is to decide whether the system is currently operating safely, critically or unsafely.

Requirements for dynamic stability techniques consist of both the computational efficiency and high accuracy. Eigenvalue analysis is one of the conventional methods in dealing with the dynamic stability problems. In this paper the stability is evaluated by calculating the eigenvalue of the system matrix in the linearized dynamic equation. However, many of analytical methods used for determination of these eigenvalues such as QR method [1] and modal analysis [2] and some other methods are discussed in [3], [4].

These methods are very time consuming and difficult. More recently the application of neural network has developed in many of engineering problems. One of these problems is determination of critical eigenvalue in a power system done by back propagation method [5] or KOHONEN neural network classifier [6].

In this paper, a different approach is proposed for dynamic stability assessment. This approach is based on Fuzzy ARTMAP network. Because of self-organized characteristic of these networks, they can be used online in

power systems for predicting stability indices. In [3] ARTMAP Network is used to evaluate the stability of power system, but it only states if power system is stable or not. It doesn't have any idea about stability indices.

This paper not only states the situation of power system from stability aspects but also computes stability margin of power system. In Section 2 the dynamic model of a power system is used and also the assessment of dynamic stability in power systems is introduced. Moreover it introduces the dynamic stability indices as a critical eigenvalue in dynamic model. Section 3 introduces a brief description of Fuzzy ARTMAP network at a level that is necessary to understand the main results of this paper. The experiments are discussed and the results are presented in section 4. Finally, the conclusions are drawn in section 5.

2. Dynamic Stability Assessment

The normal dynamic operation of a power system requires that all eigenvalues of a system to be in the left side of imaginary axis.

In a definite condition of loadflow, any power system has one critical eigenvalue, which is defined as the fastest eigenvalue that crosses imaginary axis in maximum load and maximum generation condition.

Using the S-matrix method [6], most critical eigenvalue in S-plane is regarded as maximum absolute value of eigenvalues in Z-plane.

Considering a power system under small disturbances, the linearized system state equation can be written as:

$$\overset{\bullet}{x} = A_s x \tag{1}$$

Where,

x: State variable vector

As: system matrix

Now, by assuming

 $x = [\Delta \delta, \Delta \omega, \Delta e'_q, \Delta V_A, \Delta E_{FD}, \Delta V_F]$

We have:

$$A_{s} = \begin{bmatrix} 0 & 377 & 0 & 0 & 0 & 0 & 0 \\ -\frac{K_{1}}{M} & -\frac{D}{M} & -\frac{K_{2}}{M} & 0 & 0 & 0 & 0 \\ -\frac{K_{4}}{T_{d0}} & 0 & -\frac{1}{K_{3}T_{d0}} & 0 & \frac{1}{T_{d0}} & 0 \\ -\frac{K_{A}K_{5}}{T_{A}} & 0 & -\frac{K_{A}K_{6}}{T_{A}} & -\frac{1}{T_{A}} & 0 & -\frac{K_{A}}{T_{A}} \\ 0 & 0 & 0 & -\frac{1}{T_{A}} & -\frac{K_{E}}{T_{E}} & 0 \\ 0 & 0 & 0 & -\frac{K_{F}}{T_{F}T_{E}} & -\frac{K_{E}K_{F}}{T_{E}T_{F}} & -\frac{1}{T_{F}} \end{bmatrix}$$
 (2)

The S-matrix method employs the transformation of the left half-plane into the unit circle i.e. transforming system matrix A₀ into the following matrix:

$$A_z = (A_s + hI)(A_s - hI)^{-1}$$
 (3)

Where.

Az: transformed system matrix

I: unit matrix

h: positive real number

Equation (3) indicates a mapping transformation from S-plane to Z-plane as shown in figure 1, where the difference between the stable region in S-plane and in Z-plane is given in hatched area. Figure 1(a) denotes the stable region in S-plane while figure 1(b) illustrates the same one in Z-plane. The advantage of Z-plane is that the system stability depends upon the existence of eigenvalue within the unit circle. As a result, power system dynamics is evaluated by the absolute value of most critical eigenvalue of matrix A_z.

In the S-matrix method, the power system dynamic stability can be judged by the absolute value of the most critical eigenvalue such as

$$\mu = \left| \lambda_z^{\rm M} \right| \tag{4}$$

Where λ_z^M is the most critical eigenvalue of matrix A_z . Therefore we have:

$$\begin{cases} \mu < 1 & \text{Stable} \\ \mu = 1 & \text{Critical} & \text{Stable} \\ \mu > 1 & \text{Unstable} \end{cases} \tag{5}$$

Since the method makes use of mapping of the eigenvalue from S-plane to Z-plane, the most critical eigenvalue is the one with the largest absolute value in Z-plane. Now, the power system dynamic stability can be judged by examining if the eigenvalue with the largest absolute value exist within the unit circle as shown in figure (1):

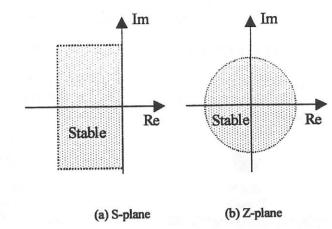


Fig. 1. Stable Region of Eigenvalues in s-plane and z-plane

3. The Fuzzy ARTMAP network

Fuzzy ARTMAP is a network with an incremental supervised learning algorithm, which combines fuzzy logic and adaptive resonance theory (ART) for recognition of pattern categories and multidimensional maps in response to input vectors presented in an arbitrary order. It realizes a new minimax learning rule, which jointly minimizes the predictive error and maximizes code compression, and therefore generalization [4].

A match tracking process that increases the ART vigilance parameter achieves this by the minimum amount needed to correct a predictive error. The Fuzzy ARTMAP neural network is composed of two Fuzzy ART modules, namely Fuzzy ART_a and Fuzzy ART_b, which are shown in figure (2).

After network is trained and clusters are created, then it is placed in parallel with power system to evaluate stability indices as shown in figure (3). The Fuzzy ARTMAP in prediction mode is shown in figure (4).

The interaction mediated by the map field F^{ab} may be operationally characterized as follows:

a) ART, and ART,

The inputs to ART_a and ART_b are in the complement code form:

For ART_a, $I=A=(a,a^c)$;

For ART_b, $I=B=(b,b^c)$;

For ARTa, let $x^a = \{x_1^a, ..., x_{2Ma}^a\}$ denotes the F_1^a output vector, $y^a = \{y_1^a, ..., y_{Na}^a\}$ denotes the F_2^a output vector, and $w_i^a = \{w_{j1}^a, ..., w_{j2Ma}^a\}$ denotes the jth ARTa weight Vector. Also for ARTb, let $x^b = \{x_1^b, ..., x_{2Mb}^b\}$ denotes the F_1^b output vector, $y^b = \{y_1^b, ..., y_{Nb}^b\}$ denotes the F_2^b output vector, and $w_k^b = \{w_{k1}^b, ..., w_{k2Mb}^b\}$ denotes the kth ARTb weight vector. For the map field, let $x^{ab} = \{x_1^{ab}, ..., x_{Nb}^{ab}\}$ denotes the F^a output vector and $w_i^{ab} = \{w_{i1}^{ab}, ..., w_{jNb}^{ab}\}$ denotes the weight vector from the jth F_2^a note to F^a .

b) Map Field Action

The map field F^{ab} is activated whenever one of the ART_a or ART_b categories is active. If node J of $F_2{}^a$ is chosen, then its weight $w_i{}^{ab}$ activate F^{ab} . If node K of $F_2{}^b$ is chosen, then the node K in F^{ab} is activated by 1-to-1 pathways between $F_2{}^b$ and F^{ab} . If both ART_a and ART_b are activated, then F^{ab} becomes active only if ART_a predicts the same category as ART_b via the weight $w_i{}^{ab}$.

The Fab output vector xab obeys the following:

$$X^{ab} = \begin{cases} y^b \Lambda W_J^{ab} & \text{if the Jth } F_2^a \text{ node is activated} \\ & \text{and } F_2^b \text{ is active} \\ W_J^{ab} & \text{if the Jth } F_2^a \text{ node is activated} \\ & \text{and } F_2^b \text{ is inactive} \\ y^b & \text{if } F_2^a \text{ is inactive} \\ & \text{and } F_2^b \text{ is active} \\ 0 & \text{if } F_2^a \text{ is inactive} \\ & \text{and } F_2^b \text{ is inactive} \end{cases}$$

$$(6)$$

By (6), $x^{ab} = 0$ if the prediction w_1^{ab} is disconfirmed by y^b . Such a mismatch event triggers an ART_a search for a better category.

c) Match tracking

At the beginning of each input presentation to the ART_a, vigilance parameter ρ_a equals a baseline vigilance ρ_{a0} . The map field vigilance parameter is ρ_{ab} . If

$$|\mathbf{x}^{ab}| < \rho_{ab} |\mathbf{y}^{b}|, \tag{7}$$

Then ρ_a is increased until it is slightly larger than $|A \wedge w_J^a| \cdot |A|^{-1}$, where A is the input to F_1^a in complement coding form. And

$$|\mathbf{x}^{\mathbf{a}}| = |\mathbf{A} \wedge \mathbf{w}_{\mathbf{J}}|^{\mathbf{a}} < \rho_{\mathbf{a}} |\mathbf{A}|, \tag{8}$$

Where J is the index of the active F₂^a node. When this occurs, ART_a search leads either to activation of another F₂^a node J with:

$$|\mathbf{x}^{\mathbf{a}}| = |\mathbf{A} \wedge \mathbf{w}_{\mathbf{J}}^{\mathbf{a}}| \ge \rho_{\mathbf{a}} |\mathbf{A}| \tag{9}$$

and

$$|x^a| = |y^b \wedge w_J^{ab}| \ge \rho_a |y^b| \tag{10}$$

Or, if no such node exists, to the shutdown of F_2^a for the remainder of the input presentation.

d) Map Field Learning

Learning rules determine how the map field weights w_{jk}^{ab} change through time. This can be done as follows: Weights w_{jk}^{ab} in $F_2^a \to F^{ab}$ paths initially satisfy: $W_{jk}^{ab}(0) = 1$

During resonance with the ART_a category J active, w_J^{ab} approaches the map field vector x^{ab} . With fast learning, once J learns to predict the ART_b category K, that association is permanent, i.e., $w_k^{ab} = 1$ for all time.

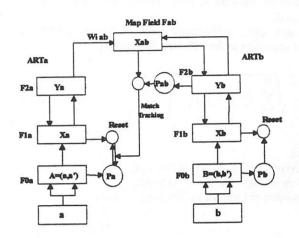


Fig.2. A typical Fuzzy ARTMAP architecture

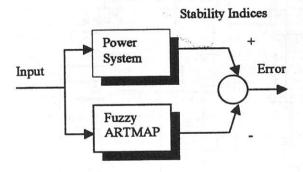


Fig.3. On-Line Training

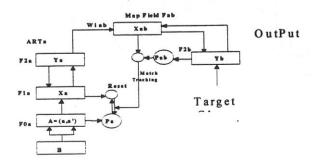


Fig.4. Fuzzy ARTMAP network for classification

4. Simulations

In order to test the algorithm for its effectiveness in predicting system security, we select a typical power system that is used in most studies. The 39 Bus New England power systems with 10 machines is tested as shown in figure (5). System configurations are available in [6], [7].

We study 6 cases in various situations and in each situation; effect of various conditions is considered. In cases of 1 through 5, we use Fuzzy ARTMAP Network and in case 6, a Perceptron Network is used. Finally the obtained results are compared.

In each case, performance error of neural network is calculated according to the following formula [6]:

$$E = \frac{1}{N} \left(\sqrt{\sum_{i=1}^{N} (y_{di} - y_{ai})^{2}} \right)$$
 (11)

Where,

y_{di}: Desired output of NeuralNetwork.
 y_{si}: Actual output of Neural Network.
 N: Number of Data Set for Training.

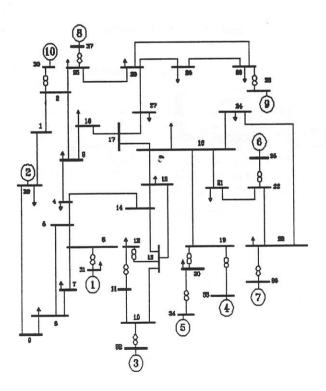


Fig.5. Typical power system

Case 1:

Using a step size of 0.05 for changing real power in both load buses and generation buses and finding critical eigenvalue, a set of 65 patterns was obtained off-line. In each step we used bus voltages ($|V_i|$, δ_i) as input bit pattern. These input bits and its respected critical eigenvalue make an input/output pair for neural network. These pairs were used to train the Fuzzy ARTMAP network. In this test, parameter ρ was chosen to be ρ_a =0.98, ρ_b =•,9 $^{\circ}$, ρ_{ab} =•,9 $^{\circ}$. A set of 6 training patterns was randomly selected from the above set. After training the network with 65 patterns, the set of 6 random patterns was used to test network. Summery of obtained results is given in table (1).

Training Error of this test is about 0.948% and is shown in figure (6).

Case 2:

In Another test we used the same number of data set, but we selected additional bit patterns as input. In this case, bus voltages and generating active power for generation buses and demanded active power for load buses ($|V_i|$, δ_i , Pg_i , Pd_i) are used as input bit patterns. Vigilance parameters are selected as above. Error obtained in this test is about 0.948% as it is seen; it is equal to Error obtained in case 1. The result is shown in figure (7).

Case 3:

In this test we used step size equal to 0.01, which creates more set of data (about 6400 set).

Also we used the same input bit patterns and the same Vigilance parameters with case 2. Error in this test is equal to 0.87%, which is a little lower than previous tests as it is shown in figure (8).

Case 4:

In this case we used 7800 set of data, and the input bit patterns are used as the one in test 1, it means $|V_i|$, δ_i . Vigilance parameters are selected as before. Error obtained in this test is the same as case 4 and is shown in figure (9).

Case 5:

In this case we used step size equal to 0.05 which creates 65 set of data. Also we used the same input bit patterns with case 2. But In this case, vigilance parameters are selected lower than before (ρ_a =0.93, ρ_b =0.92, ρ_{ab} =0.9). As it is shown in figure (10), error in this case is too higher than other cases.

Case 6 (Perceptron network):

In this case we used a 3-layer Perceptron Neural-Network with backpropagation method of training. Also we used the same input bit patterns. Error in this case is higher than the above cases and computing time for training is too high. A plot of error in this case is shown in figure (11).

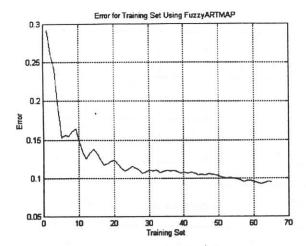


Fig.6. Error plot with 65 data set and V,delta as input (Case 1)

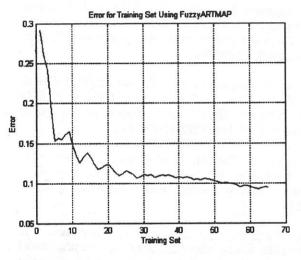


Fig.7. Error plot with 65 data set and V,delta,Pg,Pd as input (Case 2)

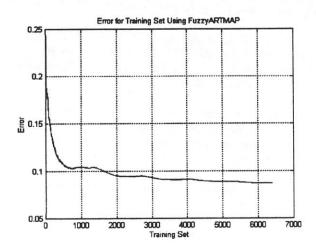


Fig. 8. Error plot with 6400 data set and V,delta,Pg,Pd as input (Case 3)

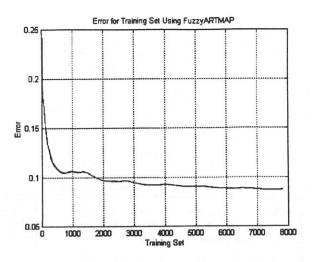


Fig.9. Error plot with 7800 data set and V,delta as input (Case 4)

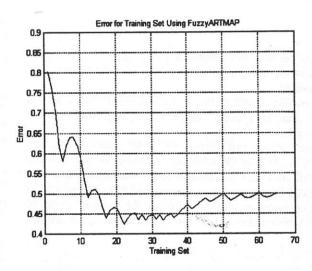


Fig.10. Error plot with 65 data set and V,delta ,pg,pd as input (Case 5)

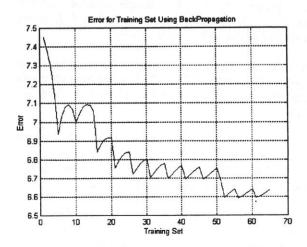


Fig.11. Error plot with 65 data set and V,delta,Pg,Pd as input (Case 6)

Network Type	Test No	Data Set No -	Input Bit patterns For Neural Network	ARTs Nede No	ARTb Node No .	pa	pb	pab	% Error
Fuzzy ARTMAP	١	٦٥	V, delta	71	۱۷	• . 4 ٨	٠.٩٧	• .97	• .90 %
	Y	70	V , delta , Pg , Pd	19	14	٠.٩٨	٠.٩٧	1.97	90%
	7	75	V, delta, Pg, Pd	٤٢٠	AYI	٠.٩٨	•.9٧	• .97	·. AY %
	£	٧٨٠٠	V , delta	٥١٨	1.7.	۸۶,۰	• .97	4,97	· . AY %
	0	מנ	V , delta , Pg , Pd	1	٤	97	• .97	4.	٤.٩٠%
" layers Percepteron	Test No .	Data Set No .	Input Bit patterns For Neural Network	Hidden Node No .	Neuron Type	Learning Rates			% Error
	7	70	V , delta , Pg , Pd	40	BSF	$n' = \gamma n = \ell_n$			٦.٧٠ %

5. Conclusion

In this paper a new approach based on Fuzzy ARTMAP NeuralNetwork for estimated dynamic stability indices has been presented.

For on-line training, the fuzzy ARTMAP network was found to that is a better choice than other neural-network training method.

It was shown that Fuzzy ARTMAP network has low sensitivity relative to the selection of number of data set feed to it for training and also relative to the number of input bits. These could be regarded as an advantage of this network. As a result a lower number of data set for training could be selected which takes less time for computing in off-line mode.

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