Converter Based Controlled Reactance for Damping Subsynchronous Resonance

Antonio C. Borré, Robson F. S. Dias, Antonio C. S. Lima, Edson H. Watanabe

Abstract—This works presents a methodology to synthesize a controlled reactance based on power electronics converter. One may understand this type of device as a *Converter Based Controlled Reactance* (CBCR) and there are several different types of controllers, but basically one main structure. As the converter performance may be affected by harmonic distortion in either voltage or current a PLL (*Phase-Locked Loop*) circuit is proposed to eliminate the effect of these distortions. The proposed CBCR can be used for reactive power compensation and to mitigate subsynchronous resonance.

The work is divided in two main parts. First, the basic structure of the CBCR is presented and then the new control is tested using "*IEEE First Benchmark*" for subsynchronous resonance. All the simulations were carried out using PSCAD/EMTDC program.

Keywords—Controllable reactances, series compensation, subsynchronous resonance (SSR), PLL (Phase-Locked Loop).

I. INTRODUCTION

Series reactive power compensation is a common procedure for increasing power transmission capability and stability conditions. Usually this can be achieved by means of series capacitor which adds a new resonance frequency to the line, normally below the grid frequency and has a very low damping factor. This type of phenomenon is commonly known as subsynchronous resonance (SSR). In some cases the SSR is not present, but electromechanical oscillations is, and this is normally in the frequency range of few Hz. To assure power reliability mitigative measures such as fast controllers, PSS (*Power System Stabilizer*) are needed. Another way to minimize power oscillations, turbine failures and sustained overvoltages during SSR or power oscillation is to include controlled reactance in series with the transmission line and this can be done by TCSC (Thyristor Controlled Series Capacitor) [1] and the SSSC (Static Series Synchronous Compensator) [2], which is based on Voltage Source Converters (VSC). The former has many examples of application in Power System throughout the world, however it has the disadvantage of including another resonance in the system while the latter is the main focus of the present work. Further details concerning TCSC and a possible way to have a simple and effective device using *Gate Controlled Switch* can be found in [3], [4].

One of the first papers dealing with synthesis of reactances using power electronics devices dates back to 1992, when the so called Variable Active-Passive Reactance (VAPAR) was presented [5], [6]. A few years later, in 1999, Hamill put forward a Bootstrap Variable Inductance (BVI) based on the concept of *bootstrapping* used in electronics devices [7], [8]. In 2004, Dranga et al. [9], [10] proposed to obtain a variable reactance from a comparison of magnetic fluxes. Later on, the same control scheme was named Active Variable Inductance [11], [12] (AVI). More recent works have focused on the concept of direct reactance synthesis DRS [13], [14]. All these control methodology can be grouped in a single converter topology. In the present work the series connection of Voltage Source Converters controlled to synthesize a controlled reactance is defined as Converter Based Controlled Reactance (CBCR).

This work is divided in two main parts, in the first the basic control principles of a CBCR are presented. A new control scheme for reactance synthesis based on a *Phase-Locked Loop* (PLL) circuit proposed in this paper is also presented. As it will be shown in the remainder of the paper a CBCR can be used to synthesize a inductive/capactive reactance including a negative inductor or capacitor. The PLL circuit adds robustness to the system as the effect of harmonic voltage/current in the converter control is reduced. To validate the proposed methodology several simulation cases are used and a comparison with previous results is shown [14]. An analysis of the CBCR for subsynchronous resonance (SSR) is also presented using the "*IEEE First Benchmark*" [15].

II. BASIC PRINCIPLES AND TOPOLOGIES OF CBCR

The main circuit of a CBCR is basically a voltage source converter behind an inductance as shown in Fig. 1. The converter can be understood as a controlled voltage source capable of controlling both amplitude and phase of the voltage fundamental component, see Fig. 2a. In steadystate, CBCR depends only on the output voltage of the VSC (\mathbf{U}_{VSC}), shown in Fig. 2a.

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A.C. Borré, R.F.S. Dias, A.C.S. Lima and E.H. Watanabe are with the Electrical Engineering Department of COPPE/UFRJ, P.O. Box. 68504, 21941-972, Rio de Janeiro, RJ, Brazil, (email:borre@coe.ufrj.br, dias@coe.ufrj.br, siqueira@coe.ufrj.br, watanabe@coe.ufrj.br).

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Assuming that $\mathbf{U}_{\mathbf{VSC}}$ and Z_L are constant, the controlled impedance can be defined as (see Fig. 2b):

$$\mathbf{Z}_{CBCR} = \frac{\mathbf{U}_T \, \mathbf{Z}_L}{\mathbf{U}_T - \mathbf{U}_{VSC}} \,. \tag{1}$$

Thus by controlling the converter voltage a controlled impedance can be obtained. In fact, the aforementioned equivalent reactance differ only in the way that the converter voltage is controlled, i.e. with a distinct set of controllers: VAPAR, BVI, AVI or DRS. All these methodologies depend on the actual line voltage/current in the line and are affected by harmonic contents in either or both. To overcome this limitation the new control algorithm based on a PLL is proposed.



Figure 1: CBCR basic structure.



Figure 2: (a) Fundamental frequency model of CBCR and (b) equivalent controlled reactance as seen from the AB terminals.

III. A New Methodology for Reactance Synthesis

As mentioned, all the controllers previously used for the variable reactance synthesis are affected by variation in the input voltage/current. Thus converters operation is limited to scenarios with low voltage/current harmonic distortion. One possibility to overcome this limitation is to use a PLL circuit as proposed by Karimi-Ghartemani and Iravani [16], [17], shown in Fig. 3. In steady-state y(t)represents the fundamental frequency component of the input x(t). The angular frequency ω_0 represents the line base frequency.

This PLL not only tracks phase but also the input signal frequency. It has an additional control loop, that detects the fundamental frequency signal magnitude for the same signal. Dynamics response for this circuit is adjusted using parameters k_1 , k_2 and k_3 , where k_1 is the main responsible for amplitude detection, and k_2 and k_3 works for obtaining phase and frequency.



Figure 3: Structure of the Karimi PLL.

With this circuit one obtains the fundamental frequency components of the line current. For this paper, the threelevel converter was chosen for synthesizing the controlled reactance, as show in Fig. 4a.



Figure 4: (a) Three-level converters and (b) control logic for converter controller.

Here also is proposed to use a three-level converter based on a *half-bridge* [18], [19], which allows a lower harmonic content in the output voltage and diminishes the stress on the semiconductor switches. The dc link voltage is controlled by u_x signal. The structure of the controller using a PLL circuit is shown in Fig. 4b, the reference voltage is given by:

$$u_{Tref}^*(t) = \omega L I_m \cos(\omega t), \qquad (2)$$

and ω is the fundamental angular frequency, L is the inductance to be synthesized by CBCR and I_m is the rms value of the current at the same frequency.

The reference voltage is obtained directly from the product of fundamental current component times ωL that is equivalent to the voltage drop across Z_{CBCR} , the synthesized equivalent reactance.

A test system using three single phase CBCR is used to evaluate the performance of the proposed control scheme when compared to DRS control. This system is depicted in Fig. 5. The parameters of the simulated system was taken from [14] and are given in Table I.



Figure 5: Simulated electrical system.

The current source in the aforementioned figure stands for a 5th order harmonic injection (with magnitude approximately equal to 10 % of the fundamental component). The goal is to assess the system performance under harmonic distortion. From 0 < t < 1 s the converter have no control order, after t = 1.0 s the control order is to synthesize a - 0.16 H (negative) inductance per phase. The converters are controlled to operate only after t = 1.0 s.

TABLE I: Circuit parameters.

Inductance: L_a	0.488 H
Resistance: R_a	17.98 Ω
Virtual inductance	-0.16 H
Voltage system 1: u_a	175.0 V
Voltage system 2: $u_{a}^{'}$	247.5 V

Fig. 6 shows the converter output voltage and the line current for phase a and Fig. 7 shows the instantaneous power and the average power flow for the system, using DRS technique.

In this Fig. 6, it is clear that CBCR is not operating correctly as we can see that approximately the voltage fundamental frequency is in phase with the current fundamental frequency. In the DRS method, theoretically, the controls tries to synthesize a perfect reactance, however the overall frequency response does not allow this.

In Fig. 7, the large ripple on the instantaneous power is due to the presence of harmonic current. After t = 1.0 s,

as the CBCR is synthesizing a negative reactance the transmitted power should increase. However due to the incorrect operation of the CBCR, this power decreases. It should be point out that the system cannot work properly with the harmonic content as the converter output voltage is heavily influenced by the 5th order harmonic in the current. DRS method synthesizes basically an equivalent reactance valid for a wide frequency spectrum, which is limited mainly by the converter frequency response.



Figure 6: Voltage and line current using DRS method.



Figure 7: Active power transfer using DRS method.

Fig. 8 shows the converter voltage and current for phase *a* using the methodology based on PLL, proposed in this paper. Fig. 9 shows the instantaneous active power as well as the average power flow.

The harmonic content does not affect the overall CBCR performance as the PLL circuit provides robustness to the converters control scheme. The use of PLL force the synthesis of the reactance to be realized in a more narrow frequency band. In fact, the PLL used assures that the equivalent reactance is synthesized at the line frequency eliminating the effect of the distortions in the voltage.

IV. IEEE BENCHMARK APPLIED TO SUBSYNCHRONOUS RESONANCE STUDIES

Series transmission lines compensations is recognized as an efficient and economic way for increasing the transmitted power. However, in some cases, special attention must be taken to avoid instability and assure reliability.

When the system may present subsynchronous resonance (SSR), this compensation has to be carefully designed otherwise it may cause mechanical or electrical problems. In some cases, the incorrect compensation causes a poor damping in some electrical oscillations that can trigger protection systems or damage the equipment.



Figure 8: Voltage and line current using the proposed technique.



Figure 9: Active power transfer using the proposed technique.

This section presents some results related to transmission line series compensation. The results were obtained using the model referred as "*First Benchmark Model for Computer Simulation of Subsynchronous Resonance*" [15], [20], shown in Fig. 10.

In this model, the generation system is a 892.4 MVA synchronous generator connected to a infinite bus across a transmission line, equipped with capacitive series compensation. This generator is driven by four turbines (two in low pressure, one in medium pressure and one in high pressure), and has additionally rotor and exciter masses [20]. In t=2.5 s, a three-phase fault is applied. This fault is simulated by connecting $X_{fault} = 13.0 \ \Omega$ between the three-phases and ground during 75 ms. In this simulation

the capacitive series compensation is $X_c = 120.7 \Omega$, which represents 75 % of the series reactance.



Figure 10: *IEEE First Benchmark* system using capacitive compensation.

The electrical torque and line current are shown in Fig. 11 and Fig. 12, respectively. Due to the series compensation after fault occurs there are low frequencies oscillations in both voltage and current.



Figure 11: Line current using capacitive compensation.



Figure 12: Generator electrical torque using capacitive compensation.

In order to analyze the ability of the CBCR to damp subsynchronous oscillations, the series capacitor bank was replaced by three single-phase CBCRs using the DRS control, as shown in Fig. 13. In this simulation the CBCR was controlled as to emulate a negative reactance with magnitude equal to the reactance of the capacitor bank in the previous case.



Figure 13: *IEEE First Benchmark* for subsynchronous resonance using the proposed technique.

The CBCR reactance order is the same as the capacitor reactance in the previous simulation. At t = 2.5 s the same three-phase fault is applied.

Fig. 14 shows the output voltage and current in converter terminals in phase a and Fig. 15 shows the machine electrical torque. The subsynchronous oscillations were mitigated using CBCR converter and the steady state is reached, as can be seen comparing Fig. 14 to Fig. 11. Fig. 14 shows that the line current is stable, however a low frequency oscillation at about 1.2 Hz appears. This oscillation is due the conventional electromechanical system. Possibly, this could be more damped by an specific power oscillation damping control like a PSS (*Power System Stabilizer*) which was not used here. During the transitory, the current in converter terminals is around 1.8 p.u. (as seen in Fig. 14b), making it necessary to overdesign the equipment or use protection mechanisms.

V. CONCLUSIONS

This work presented the basic principles for a CBCR. This controlled reactance can be used in transmission line series compensation while mitigating subsynchronous resonance. Previously proposed topologies are limited to configurations were there are low harmonic contents in the system voltage or in the line current. A simple case system was used to illustrate this limitation and a PLL circuit was proposed to allow CBCR operation in a highly distorted system.

The proposed control scheme allows to synthesize a variable reactance which can be used for reactive power compensation as well as to mitigate subsynchronous resonance. It can bring operational flexibility allowing a continuous controllable compensation. The PLL circuit provides robustness as it allows the controller to be defined only as a function of the power frequency.

To assess the proposed CBCR methodology a simple system with a high content of fifth order harmonic was used. The results are compared with the same system but using a DRS control. Although both cases aim to synthesize the same reactance only the CBCR with PLL circuit was able to do so. Thus it may be used to increase power flow transmission in highly distorted systems. However, high distortion may not appear in steady-state, it may appear during transient and therefore, the proposed methodology may be more robust in these situation.

Finally, the proposed control strategy was applied to "*IEEE First Benchmark*" to mitigate subsynchronous resonance. It provided an adequate power damping eliminating low frequency oscillations in both voltage and current.



Figure 14: (a) Voltage and current waveform at converter output and (b) line current (phase a).

References

- C. Gama, "Brazilian North-South interconnection controlapplication and operating experience with a TCSC," *IEEE Power Engineering Society Summer Meeting*, vol. 2, pp. 1103– 1108, July 1999.
- [2] A. Edris, E. H. Watanabe, P. Barbosa, P. Halvarsson, L. Angquist, B. Fardenesh, E. Uzunovic, and A. Huang, *Static Synchronous Series Compensator (SSSC)*, Feb. 2009.
- [3] L. F. Willcox de Souza, E. H. Watanabe, and M. Aredes, "GTO controlled series capacitors: multi-module and multipulse arrangements," *IEEE Trans. on Power Delivery*, vol. 15, pp. 725–731, April 2000.
- [4] L. F. Willcox de Souza, E. H. Watanabe, and J. E. Rocha Alves, "Thyristor and Gate-Controlled Series Capacitors: a comparison of components rating," *IEEE Trans. on Power Delivery*, vol. 23, pp. 899–906, April 2008.

- [5] H. Funato and A. Kawamura, "Proposal of variable activepassive reactance," *Proceedings of the International Conference* on Industrial Electronics, Control, Instrumentation and Automation, vol. 1, pp. 381–388, November 1992.
- [6] H. Funato, A. Kawamura, and K. Kamiyama, "Realization of negative inductance using Variable Active-PAssive Reactance (VAPAR)," *IEEE Trans. on Power Electronics*, vol. 12, pp. 589– 596, 1997.
- [7] D. Hamill and M. T. Bina, "The bootstrap variable inductance and its applications in AC power systems," *Applied Power Electronics Conference and Exposition (APEC '99)*, vol. 2, pp. 896–902, March 1999.
- [8] M. Tavakoli Bina and D. C. Hamill, "Bootstrap variable inductance: a new facts control element," *IEEE Annual Power Electronics Specialists Conference (PESC '99)*, vol. 2, pp. 619– 625, 1999.
- [9] O. Dranga, H. Funato, S. Ogasawara, C. Tse, and H. Iu, "Stability analysis of power circuit comprising virtual inductance," *Proceedings of the International Symposium on Circuits and* Systems (ISCAS '04), vol. 4, pp. IV-772-5, May 2004.
- [10] O. Dranga, H. Funato, S. Ogasawara, and J. Hamar, "Investigating stability of power configuration including virtual negative inductance," *IEEE 35th Annual Power Electronics Specialists Conference (PESC '04)*, vol. 4, pp. 2703–2707, 2004.
- [11] G. Ning, S. He, Y. Wang, L. Yao, and Z. Wang, "A novel distributed flexible AC transmission system controller based on Active Variable Inductance (AVI)," 37th IEEE Power Electronics Specialists Conference (PESC '06), pp. 1–4, June 2006.
- [12] —, "Design of distributed FACTS controller and considerations for transient characteristics," CES/IEEE 5th International Power Electronics and Motion Control Conference (IPEMC '06), vol. 3, pp. 1–5, August 2006.
- [13] T. E. Nuñez-Zuñiga and J. A. Pomilio, "Techniques for power negative inductance synthesis and its applications," *The 7th Brazilian Power Electronics Conference (COBEP '03)*, pp. 1–6, September 2003.
- [14] L. de Araújo Silva, "Negative inductance synthesis for series applications on the electrical network," Doctor Thesis, UNI-CAMP, March 2007.
- [15] IEEE, "First benchmark model for computer simulation of subsynchronous resonance," *IEEE Trans. on Power Apparatus and Systems*, vol. 96, pp. 1565–1572, September 1977.
- [16] M. Karimi-Ghartemani and M. R. Iravani, "A nonlinear adaptive filter for online signal analysis in power systems: applications," *IEEE Trans. on Power Delivery*, vol. 17, pp. 617–622, April 2002.
- [17] —, "A method for synchronization of power electronic converters in polluted and variable-frequency environments," *IEEE Trans. on Power Systems*, vol. 19, pp. 1263–1270, August 2004.
- [18] F. Wang, S. Rosado, T. Thacker, and D. Boroyevich, "Power electronics building blocks for utility power system applications," *Power Electronics and Motion Control Conference* (*IPEMC '04*), pp. 1–6, August 2004.
- [19] M. Steurer, "PEBB based high-power hardware-in-loop simulation facility for electric power systems," *IEEE Power Engineer*ing Society General Meeting, June 2006.
- [20] F. Domingues de Jesus, E. H. Watanabe, L. F. Willcox de Souza, and J. E. Rocha Alves, "SSR and power oscillation damping using Gate-Controlled Series Capacitor (GCSC)," *IEEE Trans.* on Power Delivery, vol. 22, pp. 1806–1812, July 2007.



Figure 15: Generator electrical torque using the proposed technique.

Antonio Carlos Borré was born in Petrópolis, Brazil. He received the B.Sc. and M.Sc. in electrical engineering from the Federal University of Rio de Janeiro (UFRJ) in 2003 and 2006, respectively. Since 2007, he has been a doctor course at with the Electrical Engineering Program of COPPE/UFRJ. His main interests include simulation and modeling of power system with FACTS equipments and DC transmission line.

Robson Francisco da Silva Dias was born in Rio de Janeiro, Brazil, in 1978. He received the B.Sc. degree in Electrical Engineering from the Federal University of Pará and Ph.D. degree in electrical engineering from the Federal University of Rio de Janeiro (UFRJ), in 2001 and 2008, respectively. Currently his is a researcher with electrical engineering department at UFRJ. His main research area includes FACTS technologies, transmission lines and electromagnetic transient studies.

Antonio Carlos Siqueira de Lima was born in Rio de Janeiro, Brazil, in 1971. He received the B.Sc., M.Sc., and Ph.D. degrees in electrical engineering from the Federal University of Rio de Janeiro (UFRJ) in 1995, 1997, and 1999, respectively. Currently, he is an Associate Professor with the Electrical Engineering Department of the UFRJ where he has been since 2002. In 1998, he was a Visiting Scholar with the Department of Electrical and Computer Engineering at the University of British Columbia, Vancouver, BC, Canada. From 2000 to 2002, he was with the Brazilian Independent System Operator, ONS, Rio de Janeiro, Brazil, dealing with electromagnetic transient studies for the Brazilian National Grid.

Edson Hirokazu Watanabe was born in Rio de Janeiro, Brazil. He received the B.Sc. degree in electronic engineering and the M.Sc. degree in electrical engineering from the Federal University of Rio de Janeiro, Rio de Janeiro, in 1975 and 1976, respectively, and the D.Eng. degree from the Tokyo Institute of Technology, Tokyo, Japan, in 1981.

In 1981, he became an Associate Professor and in 1993, became a Professor at COPPE/Federal University of Rio de Janeiro, where he teaches power electronics. His main fields of interests are converters analysis, modeling and design, active filters and FACTS.

Dr.Watanabe is a member of the Institute of Electrical Engineers Japan, the Brazilian Society for Automatic Control and the Brazilian Power Electronics Society and is a Senior Member of the Power Electronics, Industry Applications and Power Engineering Societies of IEEE. He is also a member of CIGRÈ.