

Analysis of Grey Box Modelling of Transformers

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Abstract-- Calculation of power system transients involving transformers require models that incorporate capacitive behavior. The paper outlines how classical low-frequency transformer models can be extended with capacitances and how to fit the parameters based on typical values, test report and frequency response measurements. Justified tuning factors are proposed. The responses of the models are compared to measurements in frequency domain, and with detailed black-box models in studies of transient recovery voltage and lightning. The models show reasonable agreement including the first resonance point, but with too low damping without proper adjustments.

Keywords: transformers, capacitance, scaling factors, grey-box, black-box, TRV.

I. INTRODUCTION

TRANSIENT overvoltages are one of the root causes for transformer dielectric failures [1]. CIGRE JWG A2/C4.39 "Electrical transient interaction between transformers and the power system" [2, 3] gave an overview of transient phenomena that can lead to insulation failures, such as steep-fronted waves and resonant voltage build-up. To perform transient simulations, transformer models with capacitance effects must be established. Such models can range from simple capacitance models, via classical low-frequency models with added terminal capacitances, to black-box models fitted to frequency response measurements or white-box models based on design parameters.

Grey-box transformer models are a compromise between white-box models made from design and black-box models made from measurements. The main idea is to establish a topological transformer model based on limited design-information and then tune its parameters to fit its response to (high frequency) terminal measurements. In literature, grey-box transformer models are mostly defined as RLCG ladder networks [4-7]. However, in this paper we analyze the class of grey-box models consisting of simpler engineering models extended with capacitance and damping. The aim is to discuss the impact of the available data on the transient response. Modeling guidelines can also be found in [8, 9].

This paper first outlines some simple transformer models, then presents scaling of capacitance and losses, details a specific model based on measurements and typical values, and

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finally performs an analysis of transient recovery voltage and lightning compared to a black-box model.

II. TRANSFORMER MODELING

Grey-box modeling of transformers is based on topological models fitted to measurements. This can both be simple lumped parameter model and sophisticated ladder network. In this paper the focus is on the simple, engineering models. Besides being based on limited and typically available data, these are (with exception of M2) also applicable for low-frequencies transients and are easily initialized.

A. Model topology

Figures 1-4 show the four models analyzed in this paper.

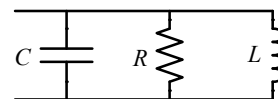


Fig. 1 M2- Artificial RLC-equivalent

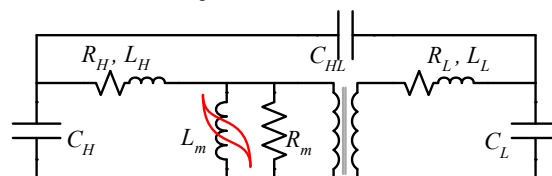


Fig. 2 M3- Simple LF-equivalent with concentrated shunt capacitances

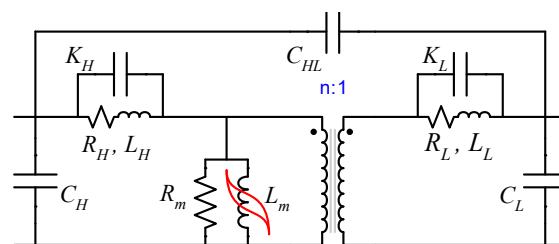


Fig. 3 M4- Simple LF-equivalent with concentrated shunt and series capacitances.

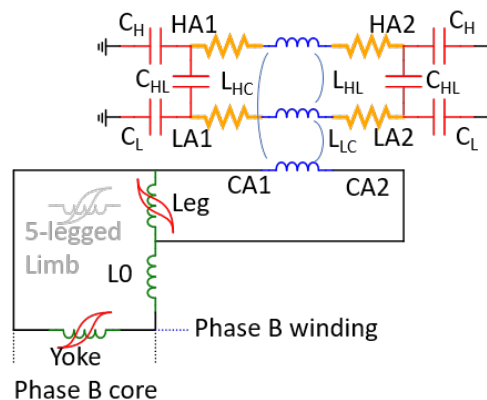


Fig. 4 M5- Three-phase model with capacitances concentrated on each side of the winding, shown for phase A.

B. Analysis of resonance frequency

The transformer model in Fig. 2 (M3) will have resonance frequencies that can be determined analytically. Referred to the HV side, the first short circuit resonance frequency of the M3 model in Fig. 2 is:

$$f_{0,sc} = \frac{1}{2\pi\sqrt{L \cdot C}} \quad (1)$$

with $L = L_H + n^2 \cdot L_L$ is the equivalent short circuit inductance and $C = C_H + C_{HL}$.

The transformer model in Fig. 3 (M4) has a series capacitor equivalent, and the short circuit resonance frequencies can also here be approximately determined analytically. If we ignore the contribution from the shorted secondary, we get:

$$f_{0\&2,M4} \approx \frac{1}{2\pi} \cdot \sqrt{\frac{2C + K_H \pm \sqrt{4C^2 + K_H^2}}{L \cdot C \cdot K_H}} \quad (2)$$

$$f_{1,M4} \approx \frac{1}{\pi \cdot \sqrt{L \cdot K_H}}$$

Based on this, the series capacitance can be estimated by utilizing the first maximum f_1 .

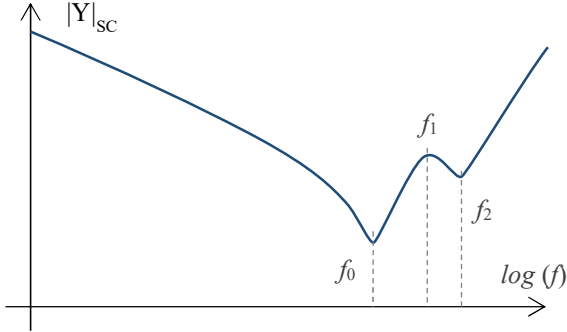


Fig. 5 Typical short circuit admittances and corresponding resonance frequencies.

Estimation of series impedance based on frequency response measurements is discussed in [10, 11]. The authors fit a ladder network model the measurements on simple transformer windings with special focus on series capacitance.

III. TRANSFORMER MODEL PARAMETERS

Grey-box transformer parameters can come from various sources categorized in typical values, test report and frequency response measurements. Some of these sources applies at power frequency others at very high frequency. Typical capacitance values found in textbook tables are usually high frequency values, while test report capacitances are given by low frequency measurements. Losses and short-circuit reactances are standardly given at power frequency. Consequently, it is necessary with a significant calibration of capacitance and losses in particular.

A. Capacitive scaling factors

The capacitances are measured at a low frequency and will contain the shunt elements only. At higher frequencies, the series capacitances become more important. The capacitance scaling factor K_s is defined as the ratio between the capacitance estimated from the first resonance frequency f_0

and the measured capacitance C_m .

$$K_s = \frac{1}{(2\pi f_0)^2 \cdot L \cdot C_m} \quad (3)$$

Horton et.al [12] suggest a scaling factor in the range of 0.3 to 0.8 with a first guess of 0.4 and state that this is well accepted. The value of the scaling factor will depend on the winding design influencing the series capacitances not measured in the standard tests.

With distributed capacitances and inductance shown in Fig. 6 the input admittance of a winding with grounded neutral becomes as shown in (4).

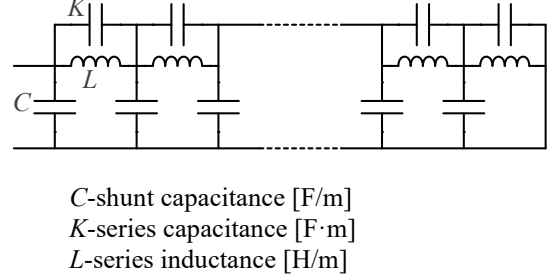


Fig. 6 Uniform single winding equivalent with distributed parameters.

$$Y_{in} = \frac{\sqrt{y/z}}{\tanh(\sqrt{z \cdot y} \cdot l)} \quad (4)$$

with $y = j\omega C$ being the shunt element, $z = j\omega L / (1 - \omega^2 LK)$ the series element and l the length of the winding and ignoring all damping. This gives the first resonance (minimum) at

$$\omega_0 = \frac{1}{\sqrt{L \cdot l \cdot (C \cdot l \cdot 4 / \pi^2 + K / l)}} \quad (5)$$

and a second minimum at

$$\omega_1 = \frac{1}{\sqrt{L \cdot l \cdot (C \cdot l \cdot 4 / (3\pi)^2 + K / l)}} \quad (6)$$

Requiring the same resonance frequency for a lumped circuit of a parallel inductor $L \cdot l$ and capacitor C_{eq} (model M2-M5) gives

$$C_{eq} = C \cdot l \cdot 4 / \pi^2 + K / l \approx C_{tot} \cdot 0.4 + K_{tot} \quad (7)$$

Cases with ignorable series capacitance K would give a scaling factor of $K_{s,K=0} = 4 / \pi^2 \approx 0.4$.

The second resonance frequency depends to a larger extend on the series capacitance. Requiring the same resonance frequency for a lumped circuit of a parallel inductor $L \cdot l$ and capacitor C_{eq} gives

$$C_{eq} = C \cdot l \cdot 4 / (3\pi)^2 + K / l \approx C_{tot} \cdot 0.045 + K_{tot} \quad (8)$$

The equivalent capacitance at very large frequencies:

$$C_{eq} = \lim_{\omega \rightarrow \infty} \frac{Y_{in}}{j\omega} = \frac{\sqrt{y/z}}{\tanh(\sqrt{z \cdot y} \cdot l) \cdot j\omega} = \frac{\sqrt{C \cdot K}}{\tanh(\sqrt{C / K} \cdot l)} \quad (9)$$

which is close to $C_{eq} \approx \sqrt{C \cdot K}$ in practical cases an in agreement with [13]. This capacitance should be chosen for a pure capacitance model.

Furthermore, 3-phase considerations must also be made to handle various winding connections. A first approach is to

concentrate capacitances on each side of the winding as shown in Fig. 4. In [14] the capacitance location is analyzed and a method of calculating equivalent capacitances taking turn-ratio and phase-shift into considerations is proposed. The general idea is that the voltage distribution is not uniform but varies linearly along the winding, making the equal split approach inaccurate. Based on this, only 1/3 of the capacitance should be connected to the Y-side terminal. This is in agreement with [13]. The scaling for winding connection is called K_Y .

B. Damping factor

The winding and core loss resistances are typically given at power frequency but will generally increase with frequency to a considerable higher value at resonance. To obtain a model suitable for TRV studies this must be taken into account.

For the RLC model M2, the inductance is the short-circuit leakage value and the capacitance could be the typical values presented in Tables 3.1-3.3. The resistance can be calculated by (10), considering a damping factor, DF in the range of 0.6-0.8 [15].

$$R = -\frac{1}{2} \cdot \frac{\pi \sqrt{L/C}}{\ln(DF)} \quad (10)$$

IV. TEST OBJECT

This section compares measured frequency response of the test transformers T1 with the response of the transformer models M2-M5. The transformer models are based on test report data, typical values, and frequency response measurements. The comparison is somewhat complicated by the fact that the measured frequency responses were performed without oil and bushings, while test-report and typical values are always given with oil and bushings included.

A. Test report

The test reports for the two test transformers are shown in Table I and II.

TABLE I
TEST REPORT FOR THE 3-PHASE TRANSFORMER, T1.

T1: 115/34.5/13.8 kV	YNyn0d	55 MVA (ONAN)
Open circuit @34.5 kV & 55 MVA	I_0 [%]	P_0 [kW]
	0.058	30.362
Short circuit; winding seq. SPT	Z_{SC} [%]	P_{SC} [kW]
P-S @ 55 MVA	7.60	101.283
P-T @ 11 MVA	3.66	16.109
S-T @ 11 MVA	5.52	17.166
Capacitance (per phase)	C_s [nF] (winding to ground)	C_m [nF] (winding to winding)
P, S, T P-S, P-T, S-T	1.267, 1.033, 4.841	8.650, 3.337, 0.097

The capacitance given in the test report are measured with floating terminals at low frequency and will only capture the shunt elements. The capacitance must thus be scaled by

factors K_S and K_Y , with $K_S=0.4$ and $K_Y=0.5$ used in this paper.

B. Typical values

The typical quantities assumed for the two transformers are shown in Table II. Values are obtained from [13, 16-18].

TABLE II
TYPICAL VALUES FOR TEST TRANSFORMERS T1.

Quantity, M2-M5	T1: 115/34.5/13.8 kV, 55 MVA
Leakage, L [%→mH]	8.5% → 54.2 mH@115 kV
Winding resistance, R [%→Ω]	0.35%→ 2.23 mΩ@115 kV
Capacitance C_P, C_S, C_T [nF]	0.75, 0.5, 1.5
Capacitance C_{PS}, C_{PT}, C_{ST} [nF]	0.75, 0.5, 0.0
Series capacitance K_H [nF]	1.0
Damping (10), DF=0.7, C= C_P+C_S	26.5 [kΩ]
Magnetization current→inductance	0.65 % → 170 H @115 kV
Core loss resistance	764 kΩ @115 kV

For typical capacitances in this 3-winding transformer, there is insufficient information to determine all quantities. From the test report it is seen that for T1 the winding sequence is S-P-T (tertiary is the outer winding) and for T2 the winding sequence is T-S-P (tertiary is the inner winding). Outer windings will have larger capacitance and capacitance between outer and inner will be small. It is further assumed a capacitive coupling factor of 0.5 which means that the mutual capacitance is similar to the capacitance to ground. Typical series capacitance is not available so a guess of a value in the same range as the shunt capacitance is assumed.

C. Frequency response measurements

The admittance matrix is measured in the frequency domain from 50 Hz to 10 MHz. The short circuit admittance is taken as the $Y_{SC}(\omega) = Y(1,1)$ element directly, while the open circuit admittance is calculated as

$$Y_{OC}(\omega) = Y(1,1) - Y(1,2:n)^T \cdot Y(2:n,2:n)^{-1} \cdot Y(1,2:n).$$

The two admittances are shown in Fig. 7 for the transformers T1. For frequency above a few hundred kilohertz, the short- and open- circuit admittance are practically equal. In Fig. 7, the short circuit admittance shows several resonance frequencies above 20 kHz with two dominant zeros at 20 kHz and 40 kHz. The open circuit admittance has a dominant zero just above 1.5 kHz and then falls in with the poles and zeros of the short circuit admittance.

To compensate for the fact that the measurements were made without bushings, a diagonal element (representing the HV bushing) of 0.5 nF is added when post-processing the measurements. The measurements were also made without oil, but this is not compensated for here.

From Fig. 7 the basic RLC elements using in M2 can be identified:

$$R = \frac{1}{Y_R} = 14.3 \text{ k}\Omega, L = \frac{1}{\omega_L \cdot Y_L} = 40 \text{ mH}, C = \frac{Y_C}{\omega_C} = 0.96 \text{ nF}$$

V. RESULTS

In this section the models are compared to the measured frequency response, besides with an established black-box model for TRV and lightning time domain studies.

A. Short-circuit comparisons

Figures 8-10 show the short-circuit admittance of the models M2-M5 compared to the measured black-box response.

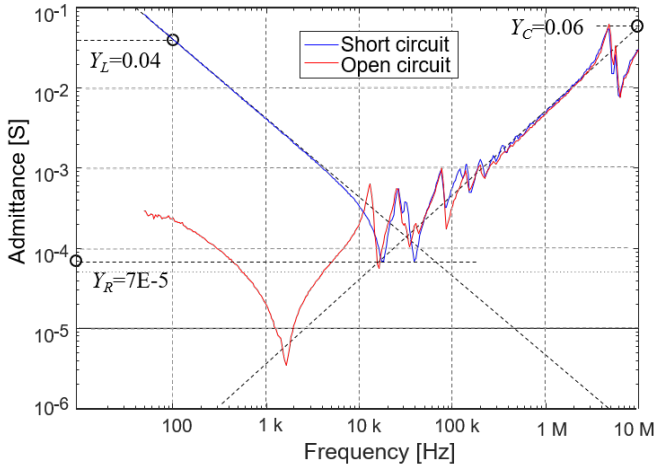


Fig. 7 Measured input admittance of phase 1 of the high-voltage winding of the 3-phase transformer, T1.

Based on (2) the series capacitance in M4 can be estimated from the second resonance. In Fig. 7 we estimate this frequency to 30 kHz and

$$K_H = \frac{1}{(\pi \cdot 30 \text{ kHz})^2 \cdot 40 \text{ mH}} = 3 \text{ nF}$$

D. Transformer models

The models are based on the Transformer Test Report, Typical Values or FRA measurements with data given in Tabl. 1-2 as given in Tabl. 3. In all cases the tertiary winding is ignored. Apparently, the capacitances of M5 are doubled, but this is due to the internal splitting of the capacitance according to Fig. 4. The capacitance on the secondary side is set qualitatively, and the same applies to typical and test-report series capacitance.

TABLE 3
TRANSFORMER T1 MODEL PARAMETERS.

Model	Test report	Typical	FRA fitted
M2	$C=1.98 \text{ nF}$ Leakage inductance (7.6%): $L=48.5 \text{ mH}$ Eq (10): $R=21.8 \text{ k}\Omega$	$C=1.5 \text{ nF}$ Leakage inductance (8.5%): $L=54.2 \text{ mH}$ Eq (10): $R=26.5 \text{ k}\Omega$	$C=0.96 \text{ nF}$ $L=40 \text{ mH}$ $R=14.3 \text{ k}\Omega$
M3	$C_p=0.253 \text{ nF}$ $C_{ps}=1.73 \text{ nF}$ $C_s=0.267 \text{ nF}$ $L=48.5 \text{ mH}$ $R=0.442 \Omega$ $R_m=436 \text{ k}\Omega$ $L_m=1837 \text{ H}$	$C_p=0.75 \text{ nF}$ $C_{ps}=0.75 \text{ nF}$ $C_s=0.5 \text{ nF}$ $L=54.2 \text{ mH}$ $R=0.805 \Omega$ (0.335%) $R_m=764 \text{ k}\Omega$ $L_m=170 \text{ H}$	$C_p=0.48 \text{ nF}$ $C_{ps}=0.48 \text{ nF}$ $C_s=0.5 \text{ nF}$ $L=40 \text{ mH}$ Damping added: $R_d=14.3 \text{ k}\Omega$
M4	Same as M3 with additional $K_H=1 \text{ nF}$	Same as M3 with additional $K_H=1 \text{ nF}$	Same as M3 with $K_H=3 \text{ nF}$. Damping across K_H of $16 \text{ k}\Omega$ and $R_d=20 \text{ k}\Omega$.
M5	$C_p=0.506 \text{ nF}$ $C_{ps}=3.46 \text{ nF}$ $C_s=0.534 \text{ nF}$ $Z_k=7.6\%$ $P_k=101.283 \text{ kW}$ $I_0=0.058\%$ $P_0=30.362 \text{ kW}$	$C_p=1.5 \text{ nF}$ $C_{ps}=1.5 \text{ nF}$ $C_s=1.0 \text{ nF}$ $Z_k=8.5\%$ $P_k=192.5 \text{ kW}$ $I_0=0.65\%$ $P_0=0$	$C_p=0.96 \text{ nF}$ $C_{ps}=0.96 \text{ nF}$ $C_s=1.0 \text{ nF}$ $Z_k=6.27\%$ $P_k=100 \text{ kW}$ $P_0=0$ Add damping $R_d=14.3 \text{ k}\Omega$

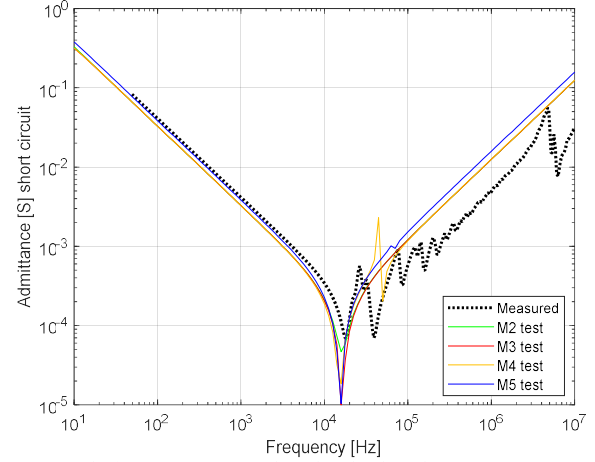


Fig. 8 T1 admittance measured and calculated, test report.

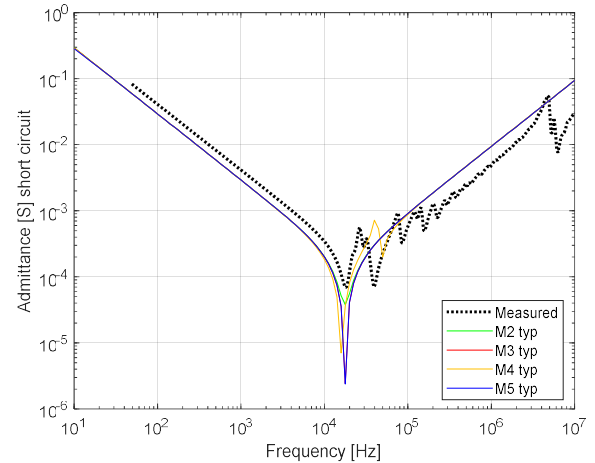


Fig. 9 T1 admittance measured and calculated, typical values.

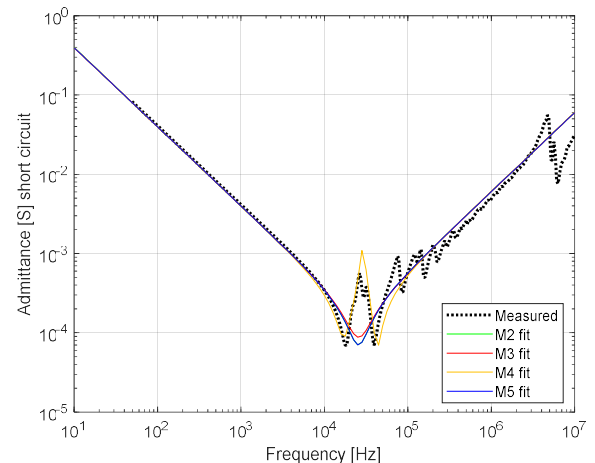


Fig. 10 T1 admittance measured and calculated, fitted parameters.

B. TRV study

The purpose is to analyze how the differences observed in the frequency domain will show up in time domain in a transient recovery voltage study. The reference (Black-box) BB-model is made from fitting the measured admittance matrix on the T1 matrix with a 120-pole model using matrix fitting toolbox [19, 20]. From Fig. 12 we see that the transformer models M2-M5 significantly overestimates the TRV peak. This is due to a far too low damping as also observed in Fig. 8. Fig. 13 shows that the over-estimated TRV-voltage is significantly reduced using fitted models with adjusted damping according to (10).

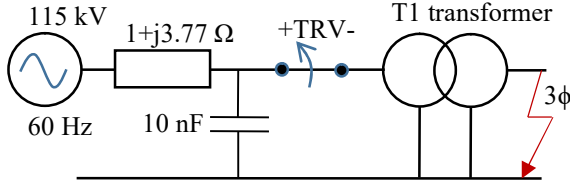


Fig. 11 Simulation of TRV with the models from Table 3.

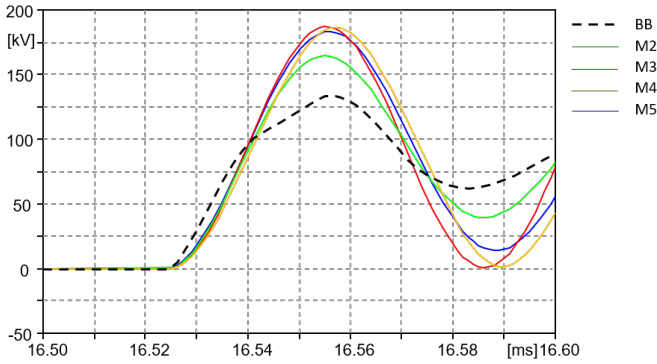


Fig. 12 Simulation result of TRV using the T1 test report transformer models from Fig. 8.

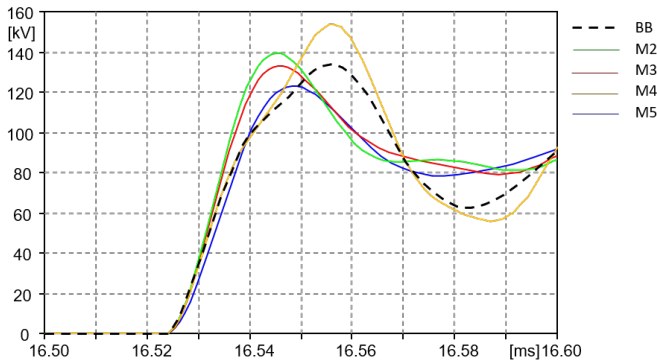


Fig. 13 Simulation result of TRV using the T1 FRA-fitted transformer models from Fig. 10.

The models M2-M5 based on test report data cannot represent well the TRV and gives too high voltage with too low damping. The M2 model has added damping and is thus the best. When fitted to frequency response measurements, all models improve with M5 as the best.

C. Lightning study

This test compares the transformer T1 models in the case of lightning strikes. This will primarily show the impact of the input impedance of the models at high frequencies (above resonance point). The lightning is assumed to hit directly in an overhead line here modelled as JMarti. The Model M2 is with the inductance disconnected.

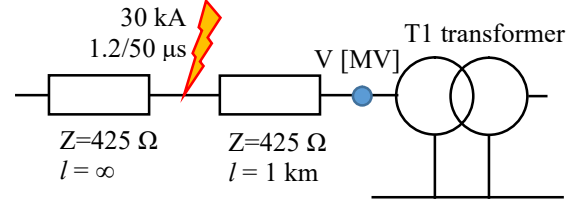


Fig. 14 Simulation of lightning overvoltages using the T1 transformer models. Open transformer secondary, M2 with disconnected inductance.

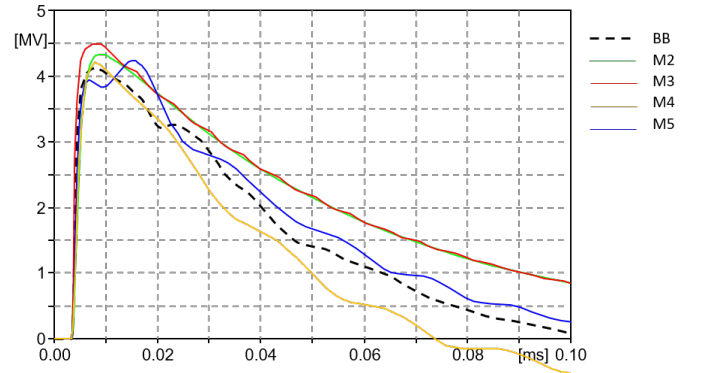


Fig. 15 Simulated lightning overvoltage at transformer terminal using the T1 test-report transformer models from Fig. 8.

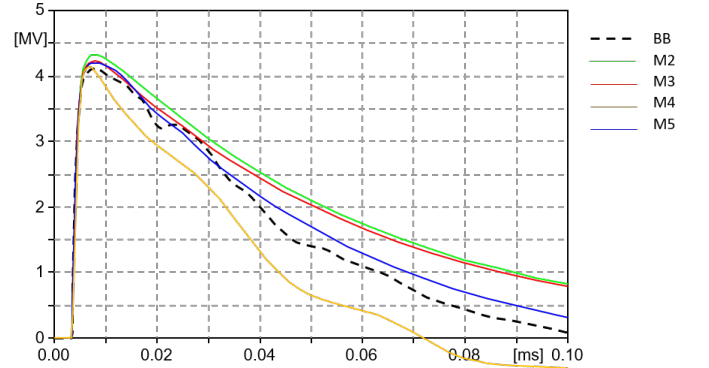


Fig. 16 Simulated lightning overvoltage at transformer terminal using the T1 fitted transformer models from Fig. 10.

For lightning studies, the models M2-M5 represent the behavior quite well, especially with fitted quantities. In this case it is the high frequency capacitive characteristics that is important.

VI. DISCUSSION

The purpose of the paper is to discuss the consequence of the available parameter values both in frequency domain and in some transient responses. The black-box model accurately fitted to frequency response measurements is taken as a reference.

Referring to Fig. 8 (Test Report), the capacitance is too

high for all the M2-M5 models. The inductance at low frequency is a bit low for the M2-M4 models. The resistive damping is good for the M2 model (always based on (10)). Referring to Fig. 9 (Typical Values), the inductance at low frequency is too low and the capacitance at high frequency is too high for all models. In Fig. 10 it is possible to fit both inductance, capacitance and damping for all models. Only the M4 model manage to capture the double resonance in the measurements, but the overall qualitative agreement is reasonable.

The simple models M2-M5 cannot represent the complex resonance behavior of the test transformers T1. The model M4 gives a better representation around resonance, but the model suffers from difficulties in estimation of the series capacitance. The 1-3 nF series capacitance used for T1 gave generally an improved performance. The over-all characteristic with a low-frequency inductive behavior and a high frequency capacitive behavior is well represented by M2-M5. The scaling of the measured capacitance with a factor 0.4 seems reasonable.

Even if the fitting is reasonable in the frequency domain, there still might be severe deviations in the time domain. The simulation of TRV shows that damping is too low for the M2-M5 models (Fig. 12) and this applies also when fitting the model to measured damping at resonance (Fig. 13). The M4 model with added and fitted series capacitance agrees with the frequency of the TRV oscillations (Fig. 13). In lightning studies (without chopping) there are less differences between the models and the M5 models gave the best match to the black-box model.

VII. CONCLUSIONS

For the transformer tested here, the qualitative agreement in the frequency domain seems reasonable matching the resonance frequency well. Still there are considerable deviations in time domain TEV studies.

- In general, the grey-box model for high frequency studies is an interesting option as it does not demand a great knowledge of the transformer design. One obvious advantage is that the models M3-M5 has a correct low-frequency behavior that make them easier to apply and initialize in general. The black-box model is in this paper used as a reference and, if available, will provide much more accurate results in transient studies.
- Depending on its structure, the simplified models can represent the behavior up to the first resonance frequency and at high frequencies. The often-complex behavior around and after the first resonance frequency is, however, not well represented by the simplified models (M2-M5). The M4 model can, in theory, represent some of the complexities at resonance but suffers from problems in estimation of the series capacitance. For a more detailed analysis of the transient behavior of the transformer, a black-box or white-box model should be considered.
- Capacitance values obtained from dielectric tests must be reduced when used in high frequency transient studies, because the series capacitances are not considered in such tests. A scaling factor in the range of 0.4 to 0.6 is recommended. The capacitances must in addition be scaled depending on the winding connections. A scaling of 1/3 to 1/2 is recommended for grounded wye.

- The consideration of damping is very important for cases where the behavior at resonance frequency dominates (for examples TRV-studies). A shunt resistance can be calculated considering a typical damping factor, the terminal leakage inductance, and the effective capacitance. The transformer models M3-M5 will have too small damping as the winding resistance is based on power frequency measurements or estimates. The resistance calculated from damping factor in (10) has shown reasonable results for the all the models.

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